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## A PARAMETRIZATION OF RATIONAL $D(q)$ -TRIPLES

Goran Dražić<sup>1</sup>, ✉

e-mail: [goran.drazic@pbf.unizg.hr](mailto:goran.drazic@pbf.unizg.hr)

**Abstract:** We parametrize rational  $D(q)$ -triples for  $q \in \mathbb{Q}$  which is not a square. We use this parametrization to describe all rational  $D(q)$ -triples which are also  $D(0)$ -triples, and to describe all rational  $D(q)$ -quadruples which contain at least one regular  $D(q)$ -triple.

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<sup>1</sup> University of Zagreb, Faculty of Food Technology and Biotechnology,  
Pierottijeva 6, Zagreb, Croatia

✉ Corresponding author

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